



# Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

### **FURTHER MATHEMATICS**

9231/43

Paper 4 Further Probability & Statistics

May/June 2024

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

## **INFORMATION**

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [ ].

This document has 12 pages.

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A college uses two assessments, X and Y, when interviewing applicants for research posts at the college. These assessments have been used for a large number of applicants this year.

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The scores for a random sample of 9 applicants who took assessment X are as follows.

21.4 24.6 25.3 22.7 20.8 21.5 22.9 21.3 22.3

The scores for a random sample of 10 applicants who took assessment *Y* are as follows.

20.9 23.5 24.8 21.9 23.4 24.0 23.8 24.1 25.1 25.8

The interviewer believes that the population median score from assessment X is lower than the population median score from assessment Y.

Carry out a Wilcoxon rank-sum test, at the 1% significance level, to test whether the interviewer's belief is supported by the data. [7]

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2	A rowing club has a large number of members. A random sample of 12 of these members is taken
	and the pulse rate, x beats per minute (bpm), of each is measured after a 30-minute training session. A
	98% confidence interval for the population mean pulse rate, $\mu$ bpm, is calculated from the sample as
	$64.22 < \mu < 68.66$ .

(a)	Find the values of $\sum x$ and $\sum x^2$ .	[6]
(b)	State an assumption that is necessary for the confidence interval to be valid.	[1]



There are three bus companies in a city. The council is investigating whether the buses reliably arrive at their destination on time. The results from random samples of buses from each company are summarised in the following table.

5

			Bus company		
		A	В	C	Total
Arrival	Early	22	22	10	54
	On time	30	52	42	124
	Late	28	26	18	72
	Total	80	100	70	250

Test, at the 5% significance level, whether the reliability of buses is independent of bus company. [7]

4 The random variable X has probability generating function  $G_X(t)$  given by

$$G_X(t) = ct(1+t)^5,$$

where c is a constant.

(a)	Find the value of $c$ .	[1]
(b)	Find the value of $E(X)$ .	[2]

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The random variable Y is the sum of two independent values of X.

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(c)	Write down the probability generating function of $Y$ and hence find $Var(Y)$ . [4]
(d)	Find $P(Y=5)$ . [2]

8

5 The continuous random variable X has cumulative distribution function F given by

$$F(x) = \begin{cases} 0 & x < 2, \\ \frac{(x-2)^2}{12} & 2 \le x < 4, \\ 1 - \frac{(8-x)^2}{24} & 4 \le x \le 8, \\ 1 & x > 8. \end{cases}$$

(a) Sketch the graph of the probability density function of X. [3]

b)	Find $E(X)$ .	[3]

2 WAR

**(c)** 

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Find the exact value of the interquartile range of $X$ .	[4]
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Seva is investigating the lengths of the tails of adult wallabies in two regions of Australia, X and Y. He chooses a random sample of 50 adult wallabies from region X and records the lengths, x cm, of their tails. He also chooses a random sample of 40 adult wallabies from region Y and records the lengths, y cm, of their tails. His results are summarised as follows.

$$\Sigma x = 1080$$
  $\Sigma x^2 = 23480$   $\Sigma y = 940$   $\Sigma y^2 = 22220$ 

It cannot be assumed that the population variances of the two distributions are the same.

of	f adult w	allabies	in region	1s X and	1 <i>Y</i> .				
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The population mean lengths of the tails of adult wallabies in regions X and Y are  $\mu_X$  cm and  $\mu_Y$  cm respectively.

r	sypothesis $\mu_Y - \mu_X > 1.1$ . State your conclusion in the context of the question.
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Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.
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